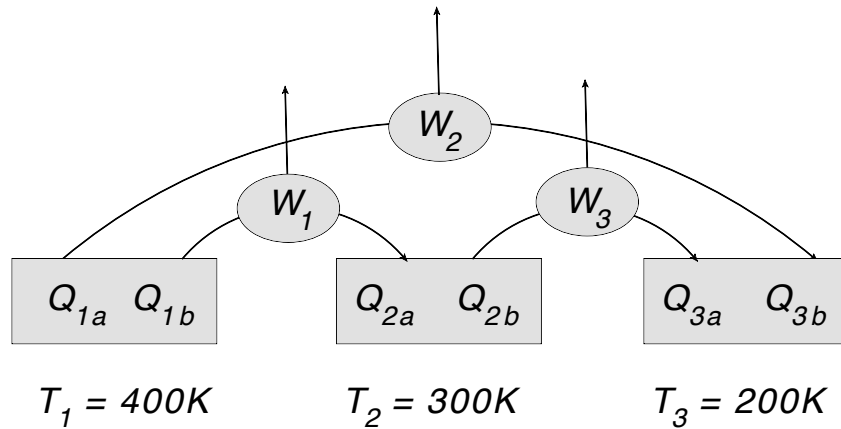


**Problem 5-7 solution**



(a)

We assume that the engines are Carnot engines, then

$$Q_{2a} = \frac{T_2}{T_1} Q_{1b} = \frac{3Q_{1b}}{4}, \quad Q_{3b} = \frac{T_3}{T_1} Q_{1a} = \frac{Q_{1a}}{2}, \quad Q_{3a} = \frac{T_3}{T_2} Q_{2b} = \frac{2Q_{2b}}{3}$$

$$\Rightarrow W_1 = Q_{1b} - Q_{2a} = \frac{Q_{1b}}{4}, \quad W_2 = Q_{2a} - Q_{3b} = \frac{Q_{1a}}{2}, \quad W_3 = Q_{2b} - Q_{3a} = \frac{Q_{2b}}{3}$$

Also,

$$Q = Q_{1a} + Q_{1b} = 1200J$$

$$W = W_1 + W_2 + W_3 = \frac{Q_{1a}}{2} + \frac{Q_{1b}}{4} + \frac{Q_{2b}}{3} = 200J$$

We get

$$W = \frac{Q_{1a}}{2} + \frac{Q_{1b}}{4} + \frac{Q_{2b}}{3} = \frac{Q_{1a} + Q_{1b}}{2} - \frac{Q_{1b}}{4} + \frac{Q_{2b}}{3} = \frac{Q}{2} - \frac{Q_{2a}}{3} + \frac{Q_{2b}}{3}$$

$$\Rightarrow Q_{2a} - Q_{2b} = 3\left(\frac{Q}{2} - W\right) = 1200J$$

$\Rightarrow$  1200J is absorbed at the second reservoir.

Next, from the overall conservation of energy

$$W = Q_{1a} + Q_{1b} - Q_{2a} + Q_{2b} - Q_{3a} - Q_{3b} = -Q_{3a} - Q_{3b} = 200J \Rightarrow -Q_{3a} + Q_{3b} = -200J$$

$\Rightarrow$  200J of heat is rejected at the third reservoir

(b), (c)

$$\Delta S_1 = -\frac{Q_{1a} + Q_{1b}}{T_1} = -3\frac{J}{K}, \quad \Delta S_2 = \frac{Q_{2a} - Q_{2b}}{T_2} = 4\frac{J}{K}, \quad \Delta S_3 = \frac{Q_{3a} + Q_{3b}}{T_3} = -1\frac{J}{K}$$

$\Rightarrow \Delta S = \Delta S_1 + \Delta S_2 + \Delta S_3 = 0$  as it should be for a reversible process.

**Problem 5-13 solution**

(a): heat engine

(b)

$$Q_{ab} = 0,$$

$$Q_{bc} = T_2(s_2 - s_1) = 250R \simeq 2.1 \times 10^6 J,$$

$$Q_{cd} = 0,$$

$$Q_{da} = T_1(s_1 - s_2) = -100R \simeq -8.3 \times 10^5 J$$

(c)

$$\eta = \frac{W}{Q_{bc}} = \frac{Q_{bc} + Q_{da}}{Q_{bc}} = \frac{T_2 - T_1}{T_2} = 60\%$$

(d)

In reverse

$$c = \frac{Q_{ad}}{Q_{bc} - Q_{ad}} = \frac{T_2}{T_2 - T_1} = \frac{2}{3} \simeq 67\%$$