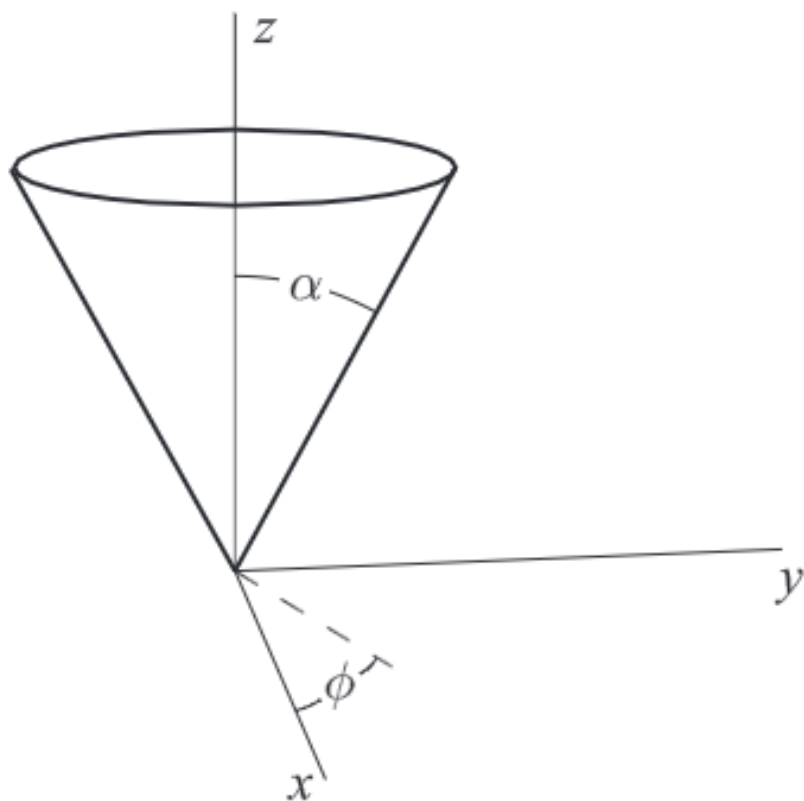


Consider a particle which is subject to gravity but constrained to move on the surface of a cone whose apex is at the origin ($x = y = z = 0$) and whose opening angle is 2α (see figure).



- Write the Lagrangian for the particle in cylindrical coordinates r, ϕ .
- Derive the equations of motion.
- Find two conserved quantities related to the motion of the particle.