

Solution to HW 3

The relevant diagrams (and the momenta flow) are shown in Fig. (1). The corresponding

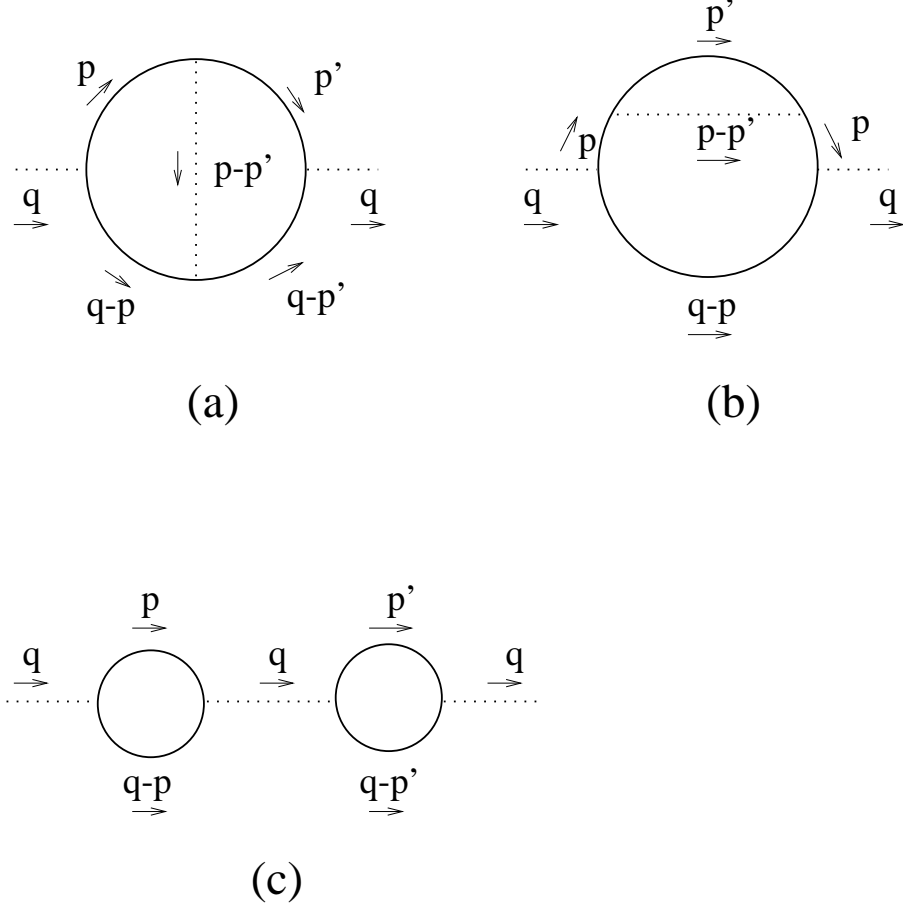


FIG. 1. Feynman diagrams for the two-pion Green function in the  $\lambda^2$  order.

expressions for the (reduced) Green functions are:

$$\mathcal{G}_a(q) = \frac{1}{2} \frac{\lambda^4}{(m^2 - q^2 - i\epsilon)^2} \int \frac{dp}{16\pi^4 i} \int \frac{dp'}{16\pi^4 i} \frac{1}{M^2 - p^2 - i\epsilon} \frac{1}{M^2 - p'^2 - i\epsilon} \frac{1}{M^2 - (q-p)^2 - i\epsilon} \frac{1}{M^2 - (q-p')^2 - i\epsilon} \frac{1}{m^2 - (p-p')^2 - i\epsilon} \quad (1)$$

for the diagram in Fig.(1)a ( $\frac{1}{2}$  is the symmetry coefficient),

$$\mathcal{G}_b(q) = \frac{\lambda^4}{(m^2 - q^2 - i\epsilon)^2} \int \frac{dp}{16\pi^4 i} \int \frac{dp'}{16\pi^4 i} \frac{1}{(M^2 - p^2 - i\epsilon)^2} \frac{1}{M^2 - p'^2 - i\epsilon} \frac{1}{M^2 - (q-p)^2 - i\epsilon} \frac{1}{m^2 - (p-p')^2 - i\epsilon} \quad (2)$$

for the diagram in Fig.(1)b (the symmetry coefficient for this diagram is 1), and

$$\mathcal{G}_c(q) = \frac{1}{4} \frac{\lambda^4}{(m^2 - q^2 - i\epsilon)^3} \int \frac{dp}{16\pi^4 i} \frac{1}{M^2 - p^2 - i\epsilon} \frac{1}{M^2 - (q-p)^2 - i\epsilon} \int \frac{dp'}{16\pi^4 i} \frac{1}{M^2 - p'^2 - i\epsilon} \frac{1}{M^2 - (q-p')^2 - i\epsilon} \quad (3)$$

for the diagram in Fig.(1)c. Here  $\frac{1}{4} = \frac{1}{2} \times \frac{1}{2}$  is the symmetry coefficient.