A particle of mass $M$ is attached by a light inextensible string of length $a$ to a small ring of mass $m$, free to slide on a fixed horizontal bar. The string moves in the vertical plane through the bar and is initially at rest at an angle $\theta$ to the vertical. Write down the Lagrangian for the system and discuss the subsequent motion.